A molecule A, present at a concentration of 1 M , decomposes irreversibly into either molecule $\mathbf{B}$ or molecule $\mathbf{C}$. The rate law for decomposition into molecule $\mathbf{B}$ is $\frac{d B}{d t}=k_{1}$ and that for molecule $\mathbf{C}$ is $\frac{d C}{d t}=$ $k_{2}[A]^{2}$. For this problem, express your answers in terms of $t, k_{1}$, and $k_{2}$.

1. Write the rate law for the rate of decomposition of $\mathbf{A}$.
2. Find the time dependence of the concentration of $\mathbf{A}$.
3. How long will it take for all of $\mathbf{A}$ to be consumed?
4. After time $t$, what is the concentration of $\mathbf{B}$ and $\mathbf{C}$ ? What is the ratio of the concentrations of $\mathbf{B}$ and $\mathbf{C}$ after the time found in part (c) elapses?

You may find the following integral useful:

$$
\int \frac{d x}{a^{2}+x^{2}}=\frac{1}{a} \arctan \frac{x}{a}+C
$$

